



Ab initio investigation of ground-states and ionic motion in particular in zirconia-based solid-oxide electrolytes

Julian Arndt Hirschfeld

Forschungszentrum Jülich GmbH
Peter Grünberg Institute (PGI)
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Contents

1. Introduction	7
2. Fuel cell functionality	13
2.1. Operating principle	13
2.2. Thermodynamic aspects	15
2.3. Fuel cell polarization	18
2.3.1. Activation overpotential	18
2.3.2. Ohmic overpotential	20
2.3.3. Concentration overpotential	21
2.3.4. The fuel cell polarization curve	21
2.4. Fuel cell efficiency	23
2.5. Fuel cell types	26
2.5.1. Proton exchange membrane fuel cell (PEMFC)	26
2.5.2. Direct methanol fuel cell (DMFC)	27
2.5.3. Alkaline fuel cell (AFC)	27
2.5.4. Solid oxide fuel cell (SOFC)	28
3. Electronic Structure Calculations	31
3.1. Density Functional Theory	31
3.1.1. Hohenberg-Kohn Theorem	32
3.1.2. Kohn-Sham Equations	34
3.1.3. Exchange-Correlation Approximations	35
3.2. Vienna Ab Initio Package (VASP)	36
3.2.1. Plane Wave Expansion and Brillouin zone sampling	36
3.2.1.1. Plane wave basis set	36
3.2.1.2. Charge density in the plane wave expansion and Brillouin zone sampling	38
3.2.2. Determining the electronic ground state	39
3.2.3. Ionic relaxation	40
3.2.4. Projector Augmented Wave Method (PAW)	43
4. Transition States and their determination	45
4.1. Transition State Theory	45
4.1.1. The diffusion rate	46
4.2. Ionic Conductivity	50
4.2.1. Crystal defects	50
4.2.2. Phenomenological description of the ionic conductivity	52

4.3.	Determination of the Transition State	53
4.3.1.	Finding the minimum energy pathway	53
4.3.2.	Nudged Elastic Band Method	54
5.	A new NEB based optimization scheme	59
5.1.	NEB in the neighborhood of a minimum	60
5.2.	The MsNEB Algorithm	62
5.3.	Applications	65
5.3.1.	Finding the most stable isomer of the P_4 cluster	66
5.3.2.	Finding the most stable isomer of the P_8 cluster	66
6.	Electrolyte materials	73
6.1.	SOFC electrolytes	73
6.1.1.	Requirements to SOFC electrolyte materials	73
6.1.2.	Yttrium Stabilized Zirconia (YSZ) and Scandium Stabilized Zirconia (SSZ)	74
6.1.3.	Other electrolyte materials under development	75
6.2.	Zirconium-dioxide ZrO_2	76
6.2.1.	Zirconia Phases	76
6.2.2.	Electronic properties of zirconia	78
6.2.3.	Charged vacancies in zirconia	79
7.	Strain Dependent migration barrier	87
7.1.	Strain dependence in ZrO_2	87
7.1.1.	Ab initio approach	87
7.1.1.1.	DFT Calculations	87
7.1.1.2.	DFT Results	89
7.1.2.	Analytic Approach	93
7.1.2.1.	Model Description	93
7.1.2.2.	Model Results	95
7.2.	Strain dependence in YSZ	97
7.2.1.	Low-doped YSZ	98
7.2.2.	High-doped YSZ	101
7.2.3.	Yttrium at the barrier position	102
7.3.	Strain dependence in SSZ	105
7.4.	Discussion of strain induced effects in doped zirconia	106
8.	Anisotropic YSZ	111
8.1.	The layered structure	111
8.2.	Stability considerations	114
8.3.	Vacancy-Vacancy interactions	117
8.4.	Molecular Dynamics	123
8.4.1.	Computational Results	124
8.5.	Conclusions	127

9. Summary	129
A. Appendix	131
A.1. Solvers for eigenvalue problems	131
A.1.1. Blocked Davidson algorithm (DAV)	131
A.1.2. Residual minimization scheme, direct inversion in the iterative sub-space (RMM-DIIS)	132
A.2. Charge mixing methods	133
A.2.1. Broyden Mixing	133
A.2.2. Kerker Mixing	134
A.3. Consideration of ion fixing for the barrier height in strained zirconium oxide	134

